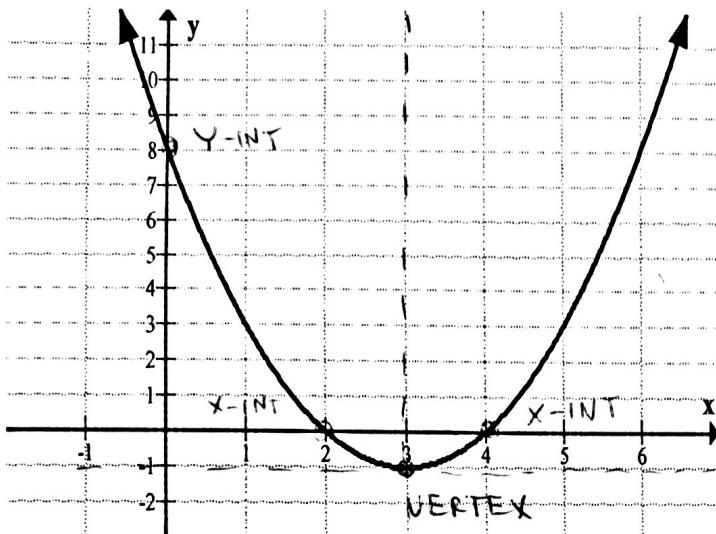


# Quadratic Relations Warmup | MFM2P

1) Identify all the key parts of the following parabola:

a)



Vertex	(3, -1)
Axis of Symmetry	$x = 3$
Optimal Value	$y = -1$
x-intercepts	(2, 0) & (4, 0)
y-intercept	(0, 8)
Direction of Opening	↑

VERTEX

2) Using your knowledge of vertex form, graph the following quadratic relations.

a)  $y = (x - 2)^2 + 1$

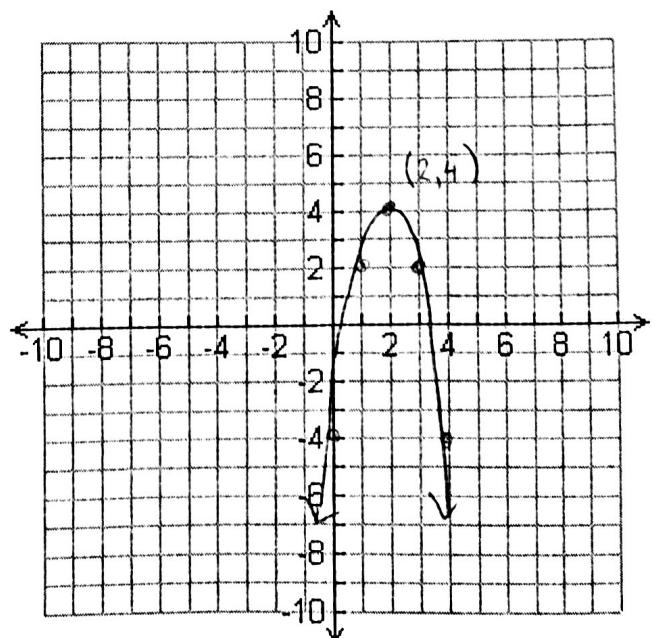
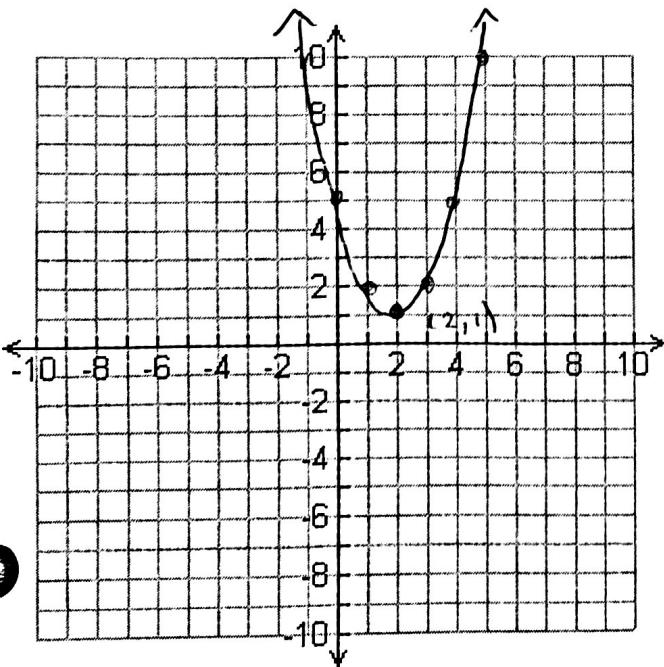
Vertex: (2, 1)

Step Pattern: 1, 3, 5

b)  $y = -2(x - 2)^2 + 4$

Vertex: (2, 4)

Step Pattern: -2, -6, -10



# Quadratic Relations Warmup | MFM2P

3) The following equations are all in vertex form:  $y = a(x - h)^2 + k$ . Complete the table.

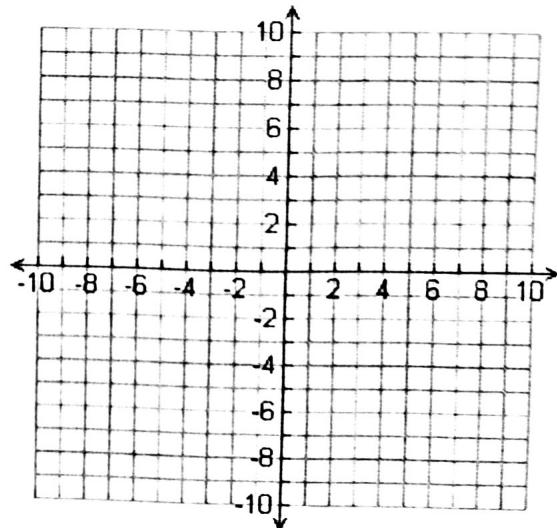
Equation	Vertex	Step Pattern
$y = (x - 2)^2 + 3$	(2, 3)	1, 3, 5
$y = 2(x - 3)^2 + 4$	(3, 4)	2, 6, 10
$y = 0.5(x + 1)^2 - 4$	(-1, -4)	0.5, 1.5, 2.5
$y = 10(x + 4)^2 + 0$	(-4, 0)	10, 30, 50

4) The following equations are all in factored form:  $y = a(x - s)(x - t)$ . Complete the table.

Equation	Zeros (x-intercepts)	Step Pattern
$y = (x - 4)(x - 6)$	(4, 0) $\downarrow$ (6, 0)	1, 3, 5
$y = 3(x + 5)(x + 1)$	(-5, 0) $\downarrow$ (-1, 0)	3, 9, 15
$y = 0.1(x - 2)(x - 3)$	(2, 0) $\downarrow$ (3, 0)	0.1, 0.3, 0.5
$y = 1000(x + 100)(x - 20)$	(-100, 0) $\downarrow$ (20, 0)	1000, 3000, 5000

5) Do you think that you could draw the parabola above?  $y = (x - 4)(x - 6)$

- Plot the zeros
- Draw the axis of symmetry
- Reason out where the vertex must be
- Finish the graph!



# Sketching From Factored Form

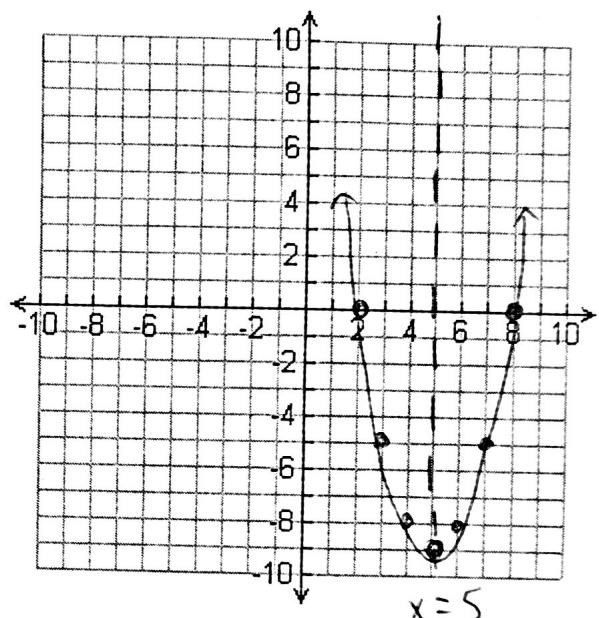
MFM2P

Today we will cement our new knowledge of factored form by sketching. Our strategy will be like the warm-up:

- Plot the zeros
- Find the axis of symmetry
- Use the axis of symmetry to find the vertex
- Finish the graph

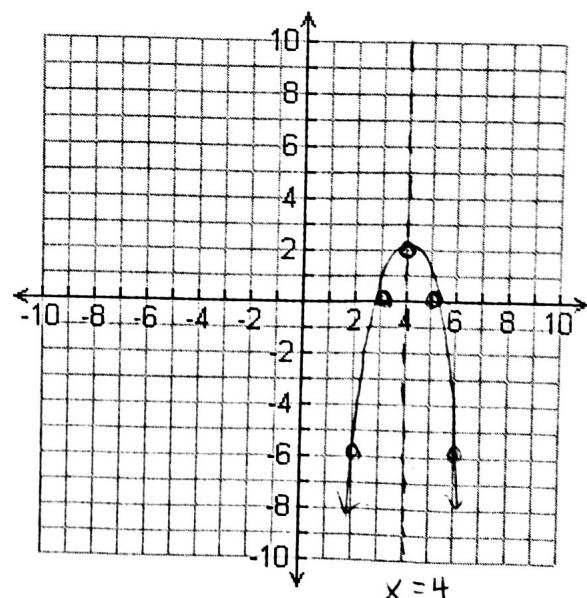
Example: Sketch the following relation on the grids provided

$y = (x - 2)(x - 8)$
Zeros: $(2, 0) \quad \{ \quad (8, 0)$
Axis of Symmetry: $x = 5$
Find the vertex: $\text{Plug in } x = 5$ $y = (5 - 2)(5 - 8)$ $= (3)(-3)$ $= -9$



Let's do one where the value of "a" is not 1.

$y = -2(x - 3)(x - 5)$
Zeros: $(3, 0) \quad \{ \quad (5, 0)$
Axis of Symmetry: $x = 4$
Find the vertex: $\text{Plug in } x = 4$ $y = -2(4 - 3)(4 - 5)$ $= -2(1)(-1)$ $= 2$



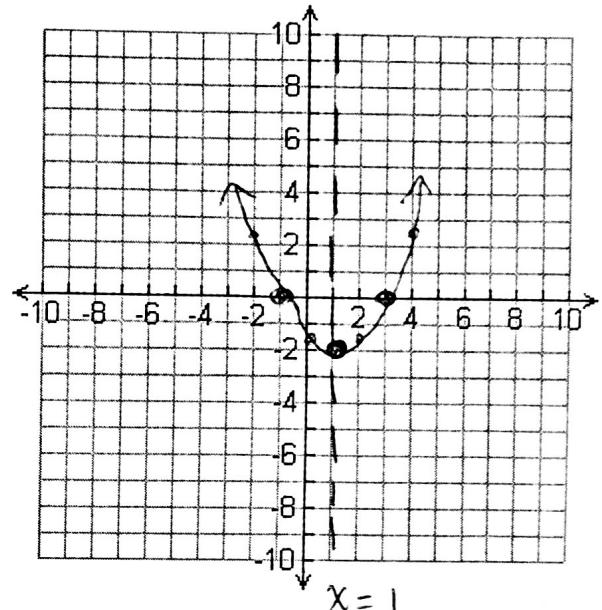
# Sketching From Factored Form

MFM2P

You try one!

$$0.5, 1.5, 2.5$$

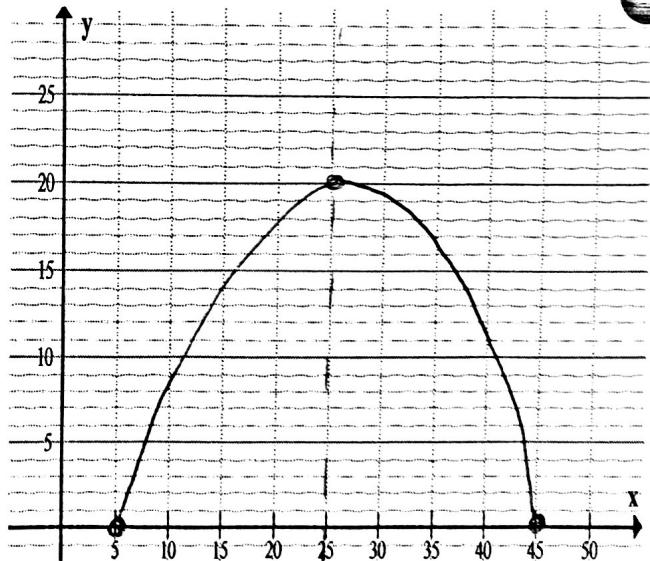
$y = 0.5(x + 1)(x - 3)$
Zeros: $(-1, 0) \quad ; \quad (3, 0)$
Axis of Symmetry: $x = 1$
Find the vertex: Sub in $x = 1$ $\begin{aligned} y &= 0.5(1+1)(1-3) \\ &= 0.5(2)(-2) \\ &= -2 \end{aligned}$



An application:

A football is punted from the 5 yard line, and lands on the 45 yard line on the same side of the field. An equation that models the flight of the ball is given by...

$y = -0.05(x - 5)(x - 45)$
Zeros: $(5, 0) \quad ; \quad (45, 0)$
Axis of Symmetry: $x = 25$
Find the vertex: Sub in $x = 25$ $\begin{aligned} y &= -0.05(25 - 5)(25 - 45) \\ &= -0.05(20)(-20) \\ &= 20 \end{aligned}$



The game is being played in an indoor dome, where the ceiling is 25m high. Will the ball hit the roof?

No, the football only reaches 20m high.