

Volume of Prisms and Pyramids | MFM2P

Today, we are going to start talking about the **volume** of 3-dimensional objects.

Volume is... the 3D space occupied by an object
units: m^3 , in^3 , ft^3 , etc...

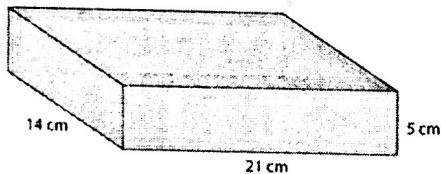
One certain type of 3-dimensional objects are called prisms. A **prism** is... a 3D shape with two identical, parallel sides (top & bottom)

KEY IDEA: To find the area of any prism...

$$\text{Volume of a prism} = \text{Area of base} \times \text{height}$$

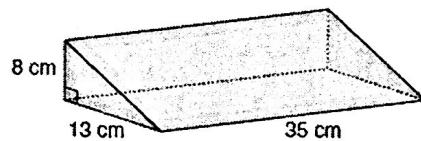
Consider the following 4 prisms. We will find their volumes.

a) A rectangular prism



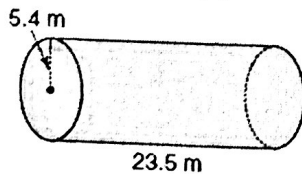
$$\begin{aligned} V &= l \times w \times h \\ &= 14 \times 21 \times 5 \\ &= 1470 \text{ cm}^3 \end{aligned}$$

b) A triangular prism



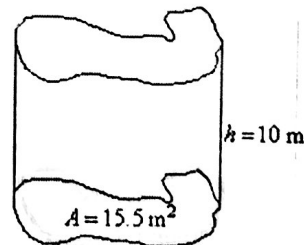
$$\begin{aligned} V &= \frac{b \times h}{2} \times l \\ &= \frac{13 \times 8}{2} \times 35 \\ &= 1820 \text{ cm}^3 \end{aligned}$$

c) A circular prism (cylinder)



$$\begin{aligned} V &= \pi r^2 h \\ &= 3.14 \times 5.4^2 \times 23.5 \\ &= 2151.7 \text{ m}^3 \end{aligned}$$

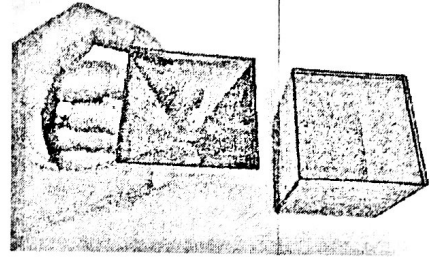
d) A prism with an irregular base



$$\begin{aligned} V &= A_{\text{base}} \times h \\ &= 15.5 \times 10 \\ &= 155 \text{ m}^3 \end{aligned}$$

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Volume of a Pyramid: In this demonstration, we are going to derive how to find the volume of a pyramid. Mr. Smith will scoop grains using a pyramid scoop, into a prism container.



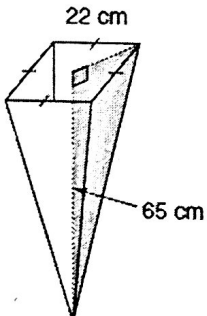
The pyramid and prism have the same base area, and height.

Predict: How many scoops do you think it will take to fill up the prism?

Observe: How many scoops did it actually take? 3 scoops

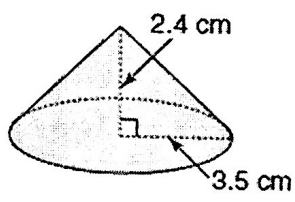
Conclusion: The volume of a pyramid is one third the volume of a prism.

Examples: Find the volume of the following pyramids with Mr. Smith

a)  $V = b^2 h \div 3$ b)

$$= 22^2 \times 65 \div 3$$

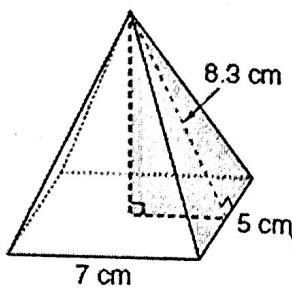
$$= 10,486.7 \text{ cm}^3$$

 $V = \pi r^2 h \div 3$

$$= 3.14 \times 3.5^2 \times 2.4 \div 3$$

$$= 30.8 \text{ cm}^3$$

c) Sometimes, we can't measure the height of a pyramid directly. In these cases, we can use the Pythagorean Theorem and their slant height.



$$h^2 = 8.3^2 - 3.5^2$$

$$= 68.89 - 12.25$$

$$= \sqrt{56.64}$$

$$h = 7.5 \text{ cm}$$

$$V = l \times w \times h \div 3$$

$$= 7 \times 5 \times 7.5 \div 3$$

$$= 87.5 \text{ cm}^3$$